

MTE - 2 - REPEAT

Question 1

(a) Briefly explain TWO (2) methods of FM generation and give ONE (1) example circuit for each of the method mentioned.

Direct method	Indirect method
<ul style="list-style-type: none">• Frequency of the carrier is varies (deviated) directly by the modulating signal.	<ul style="list-style-type: none">• Frequency-up conversion \rightarrow to up-convert the frequency of the modulated carrier after modulation has been performed.
<ul style="list-style-type: none">• The instantaneous frequency deviation is directly proportional to the amplitude of the modulating signal.	<ul style="list-style-type: none">• Two ways: Heterodyne method and Multiplication method
<ul style="list-style-type: none">• Example circuit: FM Reactance modulator, Varactor diode modulator, Linear integrated-circuit direct FM modulator	<ul style="list-style-type: none">• Example: Armstrong modulator

(b) Modulation is performed in a transmission by a circuit called a modulator. Justify FOUR (4) reasons why modulation is needed in a communication system.

- To generate a modulated signal suited and compatible to the characteristics of the transmission channel.
- For ease radiation and reduction of antenna size.
- Reduction of noise and interference
- Channel assignment
- Increase transmission speed

(c) In an Frequency Modulation (FM) system a carrier signal $V_c(t) = 20 \cos(3 \times 10^6 \pi t)$ volts is modulated by the message signal $V_m(t) = 10 \sin(62500 \pi t)$ volts and the carrier frequency varies within 5.5% of its unmodulated value. Determine

(i) Modulation Index, m_f

$$\textcircled{1} 2\pi f_c = 3 \times 10^6 \pi$$

$$f_c = 1.5 \text{ MHz}$$

$$Df = 5.5\% \times 1.5 \text{ MHz}$$

$$= \left(\frac{5.5}{100}\right) \times 1.5 \text{ MHz}$$

$$= 92.5 \text{ kHz}$$

$$Df = K V_m (Hz)$$

$$\textcircled{2} f_m = \frac{62500\pi}{2\pi} = 31.25 \text{ kHz}$$

$$\textcircled{3} \frac{Df}{f_m} = 2.64$$

(ii) Bandwidth required using Carson's rule

$$B_{FM} = 2(Df + f_m)$$

$$= 2(92.5 \text{ kHz} + 31.25 \text{ kHz})$$

$$= 227.5 \text{ kHz}$$

Question 2

(a) A telecommunication technician is given a task to access the output power levels of a conventional AM transmitter with respect to a different kind of modulation mode with the same intelligibility received. Given that the antenna transmits a 13.2 kW of total power at 75% modulation, determine:

DSBFC

(i) The total power, P_t delivered through the antenna

$$P_t = P_c + \frac{m^2}{4} P_c + \frac{m^2}{4} P_c$$

$$= 13.2 \text{ kW} + \frac{(0.75)^2}{4} (13.2 \text{ kW}) + \frac{(0.75)^2}{4} (13.2 \text{ kW})$$

$$= 16.9 \text{ kW}$$

(ii) The total power using Double-Sided Band Suppressed Carrier (DSBFC)

$$P_t = \frac{m^2}{4} P_c + \frac{m^2}{4} P_c$$

$$= \frac{0.75^2}{4} (13.2 \text{ kW}) + \frac{0.75^2}{4} (13.2 \text{ kW})$$

$$= 3.71 \text{ kW}$$

$$\textcircled{1} \text{SSBFC} \cdot P_T = P_c + \frac{m^2}{4} P_c$$

$$\textcircled{2} \text{SSBSC} \\ P_T = \frac{m^2}{4} P_c$$

(iii) The percentage of power saving of Single-Side Band Full Carrier (SSBFC) compared to Double-Side Band Full Carrier (DSBFC).

$$P_T = P_c + \frac{m^2}{4} P_c = 13.2 \text{ kW} + \frac{0.75^2}{4} (13.2 \text{ kW}) = 15.06 \text{ kW}$$

Power saving of SSBFC compared to DSBFC

$$\% P = \frac{16.9 \text{ kW} - 15.06 \text{ kW}}{16.9 \text{ kW}} \times 100\% = 10.39\%$$

(b) An AM modulated wave with the output wave changes of $\pm 7.5 \text{ V}_p$ is represented by the following equation:

$$V_m(t) = \frac{E_c}{2} \sin(2\pi 500 \times 10^3 t) + \frac{3.75 \cos(2\pi 510 \times 10^3 t) + 3.75 \cos(2\pi 490 \times 10^3 t)}{2}$$

Determine

(i) Modulation index, m and percent of modulation

$$E_{\text{max}} - E_{\text{min}} = \frac{E_m}{2} = m \frac{E_c}{2} = 3.75$$

$$\frac{m \cdot 20 \text{ V}_p}{2} = 3.75 \text{ V}_p$$

$$m = 0.375$$

$$\%m = 37.5\%$$

(ii) The peak amplitude of the modulated carrier, upper and lower side of frequency voltages.

$$E_c = 20 \text{ V}_p$$

$$E_{\text{max}} - E_{\text{min}} = 3.75 \text{ V}_p$$

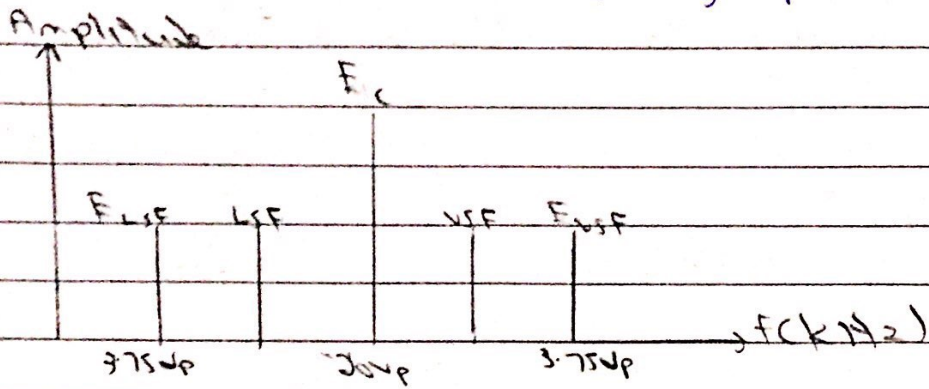
(iii) The maximum and minimum amplitude of the envelope

$$E_m = m E_c = 0.375 \times 20 = 7.5 \text{ V}_p$$

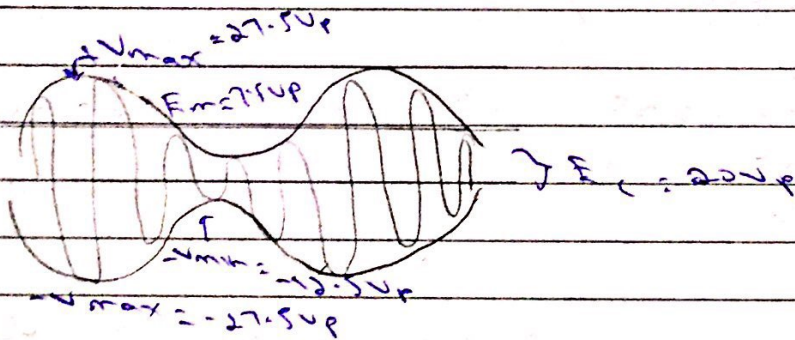
$$V_{\text{max}} = E_c + E_m = 20 \text{ V}_p + 7.5 \text{ V}_p = 27.5 \text{ V}_p$$

$$V_{\text{min}} = E_c - E_m = 20 \text{ V}_p - 7.5 \text{ V}_p = 12.5 \text{ V}_p$$

(i) Draw and label the frequency spectrum



(ii) Sketch and label the AM modulated envelope



Question 2

Write an expression for an AM voltage wave with the following values:

- Unmodulated carrier = 20 Vp
- Modulation coefficient = 0.4
- Modulating signal frequency = 5 kHz
- Carrier frequency = 200 kHz

$$\begin{aligned}
 V_m(t) &= E_c \sin(2\pi f_c t) - \frac{m E_c}{2} \cos[2\pi(f_c + f_m)t] + \\
 &\quad \frac{m E_c}{2} \cos[2\pi(f_c - f_m)t] \\
 &= 20 \sin(2\pi 200k t) - \frac{0.4(20)}{2} \cos[2\pi(200k + 5k)t] + \\
 &\quad \frac{0.4(20)}{2} \cos[2\pi(200k - 5k)t] \\
 &= 20 \sin(400\pi k t) - 4 \cos(410\pi k t) + \\
 &\quad 4 \cos(390\pi k t)
 \end{aligned}$$

(b) Given an FM modulated waveform $V_{FM}(t) = 4 \cos t$
 $(9.6 \times 10^5) \pi t + 2 \sin (27 \times 10^3) \pi t$ is transmitted through
 an antenna with a load resistance $R_L = 15 \Omega$. By referring
 to the Bessel Function Table in Appendix 1, answer the
 following questions:

(i) Determine the carrier frequency f_c , modulating frequency,
 f_m and modulation index, m_f .

$$\textcircled{1} \quad 2\pi f_c = 9.6 \times 10^5 \pi$$

$$f_c = 480 \text{ kHz}$$

$$\textcircled{2} \quad 2\pi f_m = 27 \times 10^3 \pi$$

$$f_m = 13.5 \text{ kHz}$$

$$\textcircled{3} \quad m_f = 2$$

(ii) Determine the relative amplitude of the carrier and
 side frequencies.

From Bessel Function Table,

$$m_f = 2, \quad n = 4$$

$$V_n = J_n V_c$$

$$V_0 = J_0 V_c = 0.22 \times 4 \text{ V} = 0.88 \text{ V}$$

$$V_1 = J_1 V_c = 0.58 \times 4 \text{ V} = 2.32 \text{ V}$$

$$V_2 = J_2 V_c = 0.35 \times 4 \text{ V} = 1.4 \text{ V}$$

$$V_3 = J_3 V_c = 0.13 \times 4 \text{ V} = 0.52 \text{ V}$$

$$V_4 = J_4 V_c = 0.03 \times 4 \text{ V} = 0.12 \text{ V}$$

(iii) Determine the total power in modulated carrier, P_T .

$$P_T = \frac{V_0^2}{2R} + 2 \frac{(V_1)^2}{2R} + 2 \frac{(V_2)^2}{2R} + 2 \frac{(V_3)^2}{2R} + 2 \frac{(V_4)^2}{2R}$$

$$= \frac{0.88^2}{2(15)} + 2 \frac{(2.32)^2}{2(15)} + 2 \frac{(1.4)^2}{2(15)} + 2 \frac{(0.52)^2}{2(15)} + 2 \frac{(0.12)^2}{2(15)}$$

$$= \frac{16.0299}{30}$$

$$= 0.534 \text{ W}$$

$$= 0.534 \text{ W}$$

(iv) Produce the power spectrum of the modulated output wave with their respective power amplitudes.

